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Q: Is $\lim_{x \rightarrow \infty} (1 - \cos x)^{1/x} = 1$? I'm looking for the following limit:

$$\lim_{x \rightarrow \infty} (1 - \cos x)^{1/x} = 1.$$

It's from the book Analysis I. I came up with this by first assuming it was right and

then applying L'Hospital's rule:

$$\lim_{x \rightarrow \infty} (1 - \cos x)^{1/x} = \lim_{x \rightarrow \infty} \left(\frac{(\cos x)^{-1}}{\sin x} \right) =$$

$$\lim_{x \rightarrow \infty} \left(\frac{(\cos x)^{-1}}{\cos x} \right) = \lim_{x \rightarrow \infty} \left(\frac{1}{-\sin x} \right) = \lim_{x \rightarrow \infty} (1) = 1$$

Can I do it like this? A: Recall that $1 - \cos x = 2 \sin^2 \frac{x}{2}$ so that

$$(1 - \cos x)^{1/x} = 2^{1/x} \sin^2 \frac{x}{2}$$

Take limits inside \sin (or \sin^2 for that matter). A: You can prove it directly by

using the continuity of \cos and \sin around the origin.

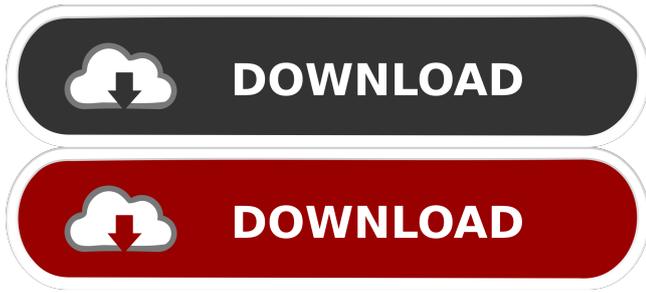
$$\lim_{x \rightarrow \infty} \left(1 - \cos x \right)^{\frac{1}{x}} = \lim_{x \rightarrow \infty} \left(\frac{1 - \cos(x)}{1 + \cos(x)} \right)^{\frac{1}{x}} = \lim_{x \rightarrow \infty} \left(\frac{1 - \cos(x)}{2} \right)^{\frac{1}{x}} = \lim_{x \rightarrow \infty} \left(\frac{2 \sin^2 \frac{x}{2}}{2} \right)^{\frac{1}{x}}$$

$$\lim_{x \rightarrow \infty} \left(\frac{1 - \cos(x)}{2} \right)^{\frac{1}{x}} = \lim_{x \rightarrow \infty} \left(\frac{2 \sin^2 \frac{x}{2}}{2} \right)^{\frac{1}{x}}$$

$$\lim_{x \rightarrow \infty} \left(\frac{1 - \cos(x)}{2} \right)^{\frac{1}{x}} = \lim_{x \rightarrow \infty} \left(\frac{2 \sin^2 \frac{x}{2}}{2} \right)^{\frac{1}{x}}$$

$$\lim_{x \rightarrow \infty} \left(\frac{2 \sin^2 \frac{x}{2}}{2} \right)^{\frac{1}{x}}$$

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Category:Music education Category:Educational psychology Category:Piano Category:Musical education Category:Music psychology Category:Cognitive musicology Category:Music education organizations Category:Educational charities based in the United States Category:Music organizations based in the United States Tuesday, November 15, 2011 SNURF SOFT SNACK GUIDE Snacks, in particular the morning ones, are an important part of a healthful lifestyle. A healthy, well-balanced breakfast can make a big difference to your day. Whole grains, fruits, and beans are key players. But if you need to go the snack route to tide you over for a bit, how can you really be smart about it? Here are some tips to keep in mind for a sensible, nutritionally sound snack. Keep a variety of whole grain foods in your refrigerator and pantry. On the health and taste front, nuts are a smart choice. Buy raw nuts, roast or bake them yourself, and shake on a little olive oil, maybe even some dried oregano. Top with a bit of lemon juice. Choose whole grain crackers, bagels or biscuits that are low in sodium. Put a bowl of grapes in the microwave and blast them until they're warm and sweet, then add a squirt of lemon juice. Have a soft, nutritious, sugar-free treat. Yogurt with a sprinkle of granola or a bowl of hot cereal (get fresh cooked oats in your refrigerator and you can make this one up on the spot) with a bit of soy milk and a dash of cinnamon is filling, and nutritious. Beans make an excellent snack when combined with whole wheat bread. Add a bit of cumin, cayenne or other seasonings to the beans, then pop them in a toaster or oven on warm. Pack a small container of hummus with carrots or celery sticks. You won't even need a bowl. Snacks are for everybody. When you have healthy alternatives ready to go, it's easy to make the switch. Try out these suggestions, and you'll be on your way to a healthy lifestyle, no matter what the occasion. Physician-centric insurance: access to care and supply-side solutions. To improve access to care, some health plans are moving toward "physician-centric" insurance. This type of plan pools the medical risk of a 2d92ce491b